

INDIAN SCHOOL DARSAIT

Class XII

Mathematics Worksheet

Worksheet # 8 Differentiability # 2

(Chapter – 5: Continuity & Differentiability)

CLASS WORK

Differentiate the following with respect to x

1.	i) $(\sin x)^{\cos x} + x^{\sin x}$ ii) $x^{\cos x} + (\cos x)^x$ iii) $x^{\sin x - \cos x} + \frac{x^2 - 1}{x^2 + 1}$ iv) $\left(x + \frac{1}{x}\right)^x + x^{\left(1+\frac{1}{x}\right)}$ v) $(\log x)^{\cos x} + \frac{x^2 + 1}{x^2 - 1}$ vi) $x^x + a^x + x^a + a^a$
2.	i) $\sqrt{\frac{(x-3)(x^2+4)}{3x^2+4x+5}}$ ii) $(x+3)^2(x+4)^3(x+5)^4$ iii) $\cos x \cdot \cos 2x \cdot \cos 3x$ iv) $(x \cos x)^x + (x \sin x)^{\frac{1}{x}}$
3.	If $x^y = y^x$, find $\frac{dy}{dx}$
4.	If $x^y \cdot y^x = 1$, prove that $\frac{dy}{dx} = \frac{y(y+x \log y)}{x(y \log x + x)}$
5.	If $e^y = y^x$, prove that $\frac{dy}{dx} = \frac{(\log y)^2}{\log y - 1}$
6.	If $(\cos y)^y = (\sin y)^x$, prove that $\frac{dy}{dx} = \frac{\log \sin y + y \tan x}{\log \cos x - x \cot y}$
7.	If $x^y = e^{x-y}$, prove that $\frac{dy}{dx} = \frac{\log x}{(\log(xe))^2}$
8.	If $x^p y^q = (x+y)^{p+q}$, prove that $\frac{dy}{dx} = \frac{y}{x}$
9.	If $x^{16} y^9 = (x^2 + y)^{17}$, prove that $x \frac{dy}{dx} = 2y$
10.	Find $\frac{dy}{dx}$ if $x^y + y^x = \log a$
11.	If $x^y + y^x = (x+y)^{x+y}$, find $\frac{dy}{dx}$
12.	If $y = \sqrt{\sin x + \sqrt{\sin x + \sqrt{\sin x = \infty}}}$, prove that $\frac{dy}{dx} = \frac{\cos x}{2y-1}$
13.	If $y = \sin x^{\sin x^{\sin x^{\sin x^{\dots \infty}}}}$, prove that $\frac{dy}{dx} = \frac{y^2 \cot x}{1 - y \log \sin x}$
14.	If $y = a^{x^{a^x^{\dots^{\infty}}}}$, prove that $\frac{dy}{dx} = \frac{y^2 \log y}{x(1 - y \log x \log y)}$
15.	If $y = \frac{\sin x}{1 + \frac{\cos x}{1 + \frac{\sin x}{1 + \frac{\cos x}{1 + \dots \infty}}}}$, prove that $\frac{dy}{dx} = \frac{(1+y)\cos x + y \sin x}{1 + 2y + \cos x - \sin x}$

HOME WORK

Differentiate the following with respect to x :-

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Mathematics Worksheet

Worksheet # 8 Differentiability # 2

(Chapter – 5: Continuity & Differentiability)

16.	$(\cos x)^x + (\sin x)^{\frac{1}{x}} x^{\sin^{-1} x} x^{\cos x} + \sin x^{\tan x} (\sin x)^x + \sin^{-1} \sqrt{x} (\sin x - \cos x)^{\sin x - \cos x} x^{x^2 - 3} + (x - 3)^{x^2}$ $x^{\cos x} + \frac{x^2 + 1}{x^2 - 1} 10^{10^x} \sin(x^x),$
17.	If $y = a^x + e^x + x^x + x^a$, find $\frac{dy}{dx}$
18.	If $x^m \cdot y^n = 1$, prove that $\frac{dy}{dx} = \frac{-my}{nx}$
19.	Find $\frac{dy}{dx}$ if $(\cos x)^y = (\cos y)^x$
20.	If $(\cos x)^y = (\tan x)^y$, prove that $\frac{dy}{dx} = \frac{\log \tan y + y \tan x}{\log \cos x - x \sec y \cos ec y}$
21.	If $x^{13} y^7 = (x+y)^{20}$, prove that $\frac{dy}{dx} = \frac{y}{x}$
22.	If $e^x + e^y = e^{x+y}$, prove that $\frac{dy}{dx} = -e^{y-x}$
23.	Given $y = \cos\left(\frac{x}{2}\right) \cdot \cos\left(\frac{x}{4}\right) \cdot \cos\left(\frac{x}{8}\right) \dots = \frac{\sin x}{x}$, prove that $\frac{1}{2^2} \sec^2 \frac{x}{2} + \frac{1}{2^4} \sec^2 \frac{x}{4} + \frac{1}{2^8} \sec^2 \frac{x}{8} + \dots = \cos ec^2 x - \frac{1}{x^2}$
24.	Find $\frac{dy}{dx}$ if $x^y + y^x + x^x = a^b$
25.	Differentiate $\log(x^x + \operatorname{Cos ec}^2 x)$
26.	If $x^y \cdot y^x = 1$, prove that $\frac{dy}{dx} = \frac{y(y+x \log y)}{x(x+y \log x)}$
27.	If $y = e^{x+e^{x+e^{x+\dots}}} \dots$, prove that $\frac{dy}{dx} = \frac{y}{1-y}$
28.	If $y = \sqrt[x]{x} \dots$, prove that $\frac{dy}{dx} = \frac{y^2}{x(2-y \log x)}$

SELF STUDY

29.	If $x^y = y^x$, find $\frac{dy}{dx}$
30.	Find $\frac{dy}{dx}$ if $y = x^x - 2^{\sin x}$
31.	If $y = \operatorname{Tan} x^{x^{\tan x^{\tan x^{\dots}}}}$, prove that $\frac{dy}{dx} = 2$ at $x = \frac{\pi}{4}$
32.	Find $\frac{dy}{dx}$ if $y = 10^{x^{10^x}}$